

Programming Paradigms

Syntax (Part 2)

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Overview

- **Specifying syntax**

- Regular expressions
- Context-free grammars



- **Scanning**

- **Parsing**

Are regular expressions enough?

Specifying arithmetic expressions

↳ E.g.:

$$\begin{array}{l} 5 + 7 \\ (5 + 7) + 6 \\ ((5 + 7) + 6) - 23 \end{array}$$

Each is an arithmetic expression

→ Want: Nesting

→ Need recursion

Context-free Grammars

≈ **Regular expressions + Recursion**

Example: Arithmetic expressions

expr → **id** | **number** | **expr op expr** | **(expr)**

op → **+** | **-** | ***** | **/**

Context-free Grammars

≈ Regular expressions + Recursion

Example: Arithmetic expressions

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Non-terminals



Context-free Grammars

≈ Regular expressions + Recursion

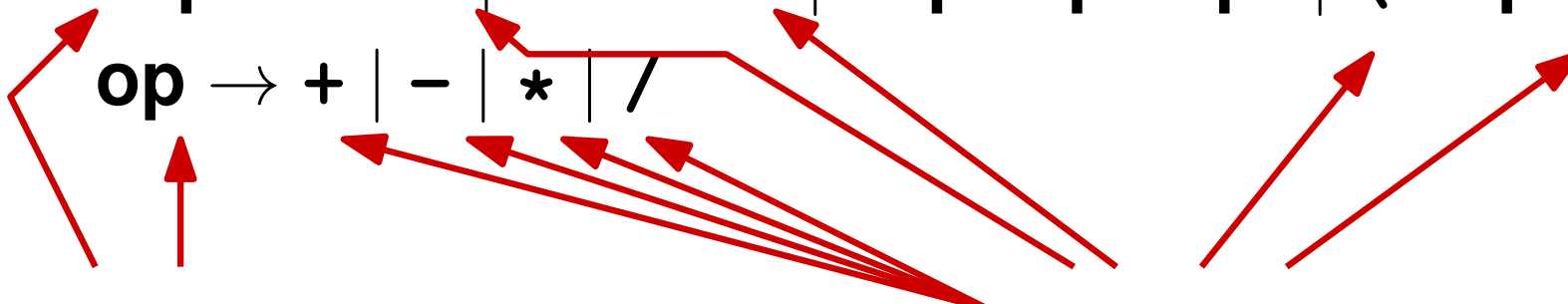
Example: Arithmetic expressions

expr → **id** | **number** | **expr op expr** | **(expr)**

op → **+** | **-** | ***** | **/**

Non-terminals

**Terminals =
tokens of the PL**



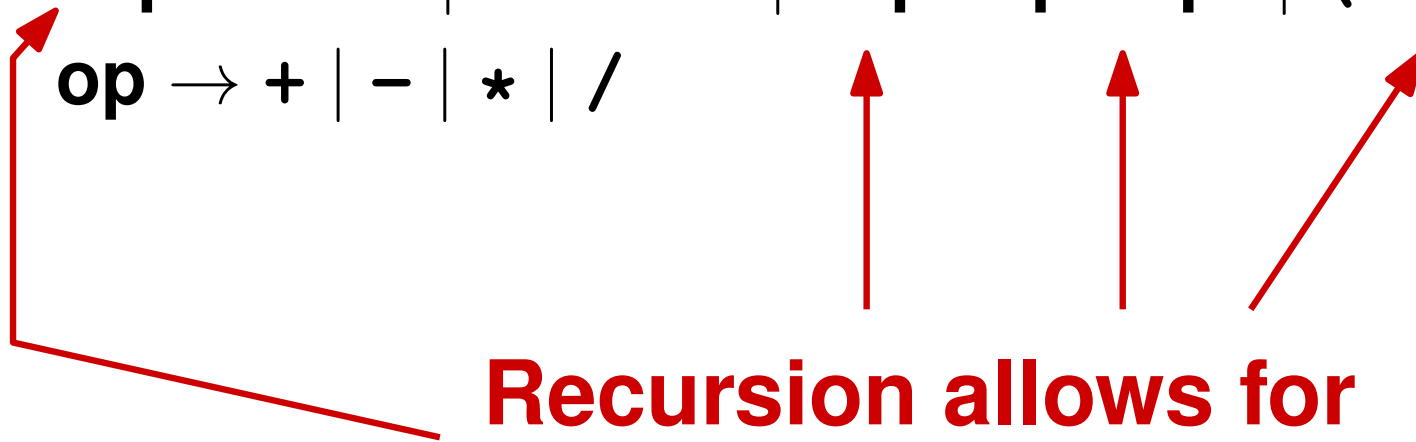
Context-free Grammars

≈ Regular expressions + Recursion

Example: Arithmetic expressions

$\text{expr} \rightarrow \text{id} \mid \text{number} \mid \text{expr op expr} \mid (\text{expr})$

$\text{op} \rightarrow + \mid - \mid * \mid /$



Recursion allows for nesting expressions

Definition of CFGs

$$G = (N, T, R, s)$$

N .. finite set of non-terminals

T .. finite set of terminal
 = alphabet of the language
 = (for PLs) tokens of the language

R .. finite relation from N to $(N \cup T)^*$
 = production rules

s .. start symbol

Extension of basic definition

- Kleene star

↳ E.g., $id_list \rightarrow id (, id)^*$ ←----- means zero & more

↳ short-hand for

$id_list \rightarrow id$

$id_list \rightarrow id_list, id$

- Kleene plus

↳ Same, but one or more

- Vertical bar

↳ E.g., $op \rightarrow + | - | * | /$

↳ Short-hand for $op \rightarrow +$

$op \rightarrow -$

⋮

Derivations

Create concrete strings from the grammar

- Begin with start symbol
- Repeat until no non-terminals remain:
 - Choose non-terminal and a production with this non-terminal on the left-hand side
 - Replace it with right-hand side of the production (choose one option if multiple options)

Example:

$\text{expr} \rightarrow \text{id} \mid \text{number} \mid \text{expr} \mid (\text{expr}) \mid \text{expr op expr}$

$\text{op} \rightarrow + \mid - \mid * \mid /$

Derivation of $\text{foo} * x + \text{bar}$

$\text{expr} \Rightarrow \text{expr op expr}$

$\Rightarrow \text{expr op id}$

$\Rightarrow \text{expr} + \text{id}$

$\Rightarrow \text{expr op expr} + \text{id}$

$\Rightarrow \text{expr op id} + \text{id}$

$\Rightarrow \text{expr} * \text{id} + \text{id}$

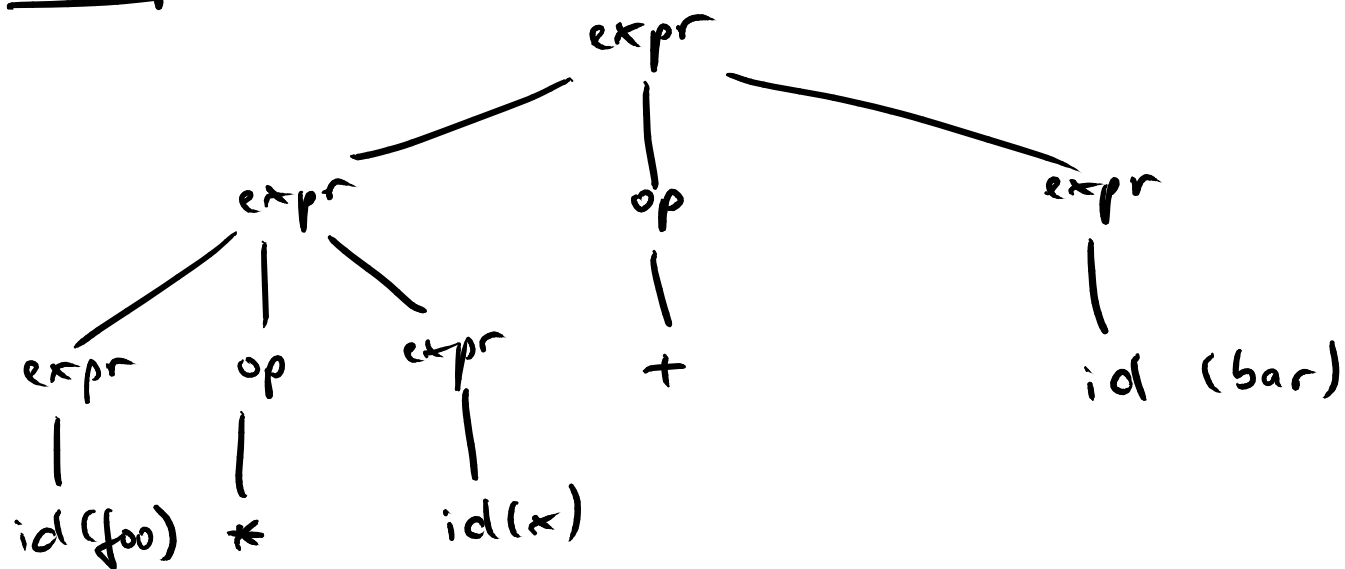
$\Rightarrow \text{id} * \text{id} + \text{id}$

$\text{foo} \quad x \quad \text{bar}$

Parse Trees

Tree-structured representation of a derivation

- Root = Start symbol
- Leaf nodes = Tokens that result from derivation
- Intermediate nodes = Application of a production

Example

Not All Grammars are Equal

Each language has **infinitely many grammars**

Some grammars are **ambiguous**

- A single string may have multiple derivations
- Unambiguous grammars facilitate parsing

Grammar should **reflect the internal structure** of the PL

- E.g., associativity and precedence of operators

Example: Revised Grammar

A better version of the grammar of arithmetic expressions:

expr \rightarrow term | expr add_op term

term \rightarrow factor | term mult_op factor

factor \rightarrow id | number | - factor | (expr)

add_op \rightarrow + | -

mult_op \rightarrow * | /

Quiz: Context-free Grammars

Draw the parse tree of $\text{foo} * x + \text{bar}$ with the revised grammar. How many nodes and edges does the tree have?

Please vote via Ilias.

Solution of quiz :

